

Squeezed particle-antiparticle correlations*

SANDRA S. PADULA, DANUCE M. DUDEK,

IFT-UNESP, Rua Pamplona, 145, 01405-900 São Paulo, SP, Brazil

AND

OTÁVIO SOCOLOWSKI JR.

IMEF - FURG - C. P. 474, 96201-900, Rio Grande, RS, Brazil

A novel type of correlation involving particle-antiparticle pairs was found out in the 1990's. Currently known as squeezed or Back-to-Back Correlations (BBC), they should be present if the hadronic masses are modified in the hot and dense medium formed in high energy heavy ion collisions. Although well-established theoretically, such hadronic correlations have not yet been observed experimentally. In this phenomenological study we suggest a promising way to search for the BBC signal, by looking into the squeezed correlation function of $\phi\phi$ and K^+K^- pairs at RHIC energies, as function of the pair average momentum, $\mathbf{K}_{12} = (\mathbf{k}_1 + \mathbf{k}_2)/2$. The effects of in-medium mass-shift on the identical particle correlations (Hanbury-Brown & Twiss effect) are also discussed.

PACS numbers: 25.75.Gz, 25.75.-q, 21.65.Q, 21.65.Jk

1. Introduction

The hadronic particle-antiparticle correlation was already pointed out in the beginning of the nineties. However, the final formulation of these hadronic squeezed or back-to-back correlations was proposed only at the end of that decade[1], predicting that such correlations were expected if the masses of the mesons were modified in the hot and dense medium formed in high energy nucleus-nucleus collisions. Soon after that, it was shown that analogous correlations would exist in the case of baryons as well. An interesting theoretical finding was that both the fermionic (fBBC) and the bosonic (bBBC) Back-to-Back Correlations were very similar, both being

* Presented at the IV Workshop on Particle Correlations and Femtoscopy (WPCF 2008), Krakow, Poland, September 11-14, 2008.

positive and treated by analogous formalisms. In what follows, we will focus our discussion to the bosonic case, illustrating the effect by considering $\phi\phi$ and K^+K^- pairs, considered to be produced at RHIC energies[3].

Let us discuss the case of ϕ -mesons first, which are their own antiparticles, and suppose that their masses are modified in hot and dense medium. Naturally, they recover their asymptotic masses after the system freezes-out. Therefore, the joint probability for observing two such particles, i.e., the two-particle distribution, $N_2(\mathbf{k}_1, \mathbf{k}_2) = \omega_{\mathbf{k}_1} \omega_{\mathbf{k}_2} \langle a_{\mathbf{k}_1}^\dagger a_{\mathbf{k}_2}^\dagger a_{\mathbf{k}_2} a_{\mathbf{k}_1} \rangle$, can be factorized as $N_2(\mathbf{k}_1, \mathbf{k}_2) = \omega_{\mathbf{k}_1} \omega_{\mathbf{k}_2} \left[\langle a_{\mathbf{k}_1}^\dagger a_{\mathbf{k}_1} \rangle \langle a_{\mathbf{k}_2}^\dagger a_{\mathbf{k}_2} \rangle + \langle a_{\mathbf{k}_1}^\dagger a_{\mathbf{k}_2} \rangle \langle a_{\mathbf{k}_2}^\dagger a_{\mathbf{k}_1} \rangle + \langle a_{\mathbf{k}_1}^\dagger a_{\mathbf{k}_2}^\dagger \rangle \langle a_{\mathbf{k}_2} a_{\mathbf{k}_1} \rangle \right]$, after applying a generalization of Wick's theorem for locally equilibrated systems[4, 5]. The first term corresponds to the product of the spectra of the two ϕ 's, $N_1(\mathbf{k}_i) = \omega_{\mathbf{k}_i} \frac{d^3 N}{d\mathbf{k}_i} = \omega_{\mathbf{k}_i} \langle a_{\mathbf{k}_i}^\dagger a_{\mathbf{k}_i} \rangle$, being $a_{\mathbf{k}}^\dagger$ and $a_{\mathbf{k}}$ the free-particle creation and annihilation operators of scalar quanta, and $\langle \dots \rangle$ means thermal averages. The second term contains the identical particle contribution and is represented by the square modulus of the chaotic amplitude, $G_c(\mathbf{k}_1, \mathbf{k}_2) = \sqrt{\omega_{\mathbf{k}_1} \omega_{\mathbf{k}_2}} \langle a_{\mathbf{k}_1}^\dagger a_{\mathbf{k}_2} \rangle$. Together with the first term, it gives rise to the femtoscopic or Hanbury-Brown & Twiss (HBT) effect. The third term, the square modulus of the squeezed amplitude, $G_s(\mathbf{k}_1, \mathbf{k}_2) = \sqrt{\omega_{\mathbf{k}_1} \omega_{\mathbf{k}_2}} \langle a_{\mathbf{k}_1} a_{\mathbf{k}_2} \rangle$, is identically zero in the absence of in-medium mass-shift. However, if the particle's mass is modified, together with the first term it leads to the squeezing correlation function.

The annihilation (creation) operator of the asymptotic, observed bosons with momentum $k^\mu = (\omega_k, \mathbf{k})$, a (a^\dagger), is related to the in-medium annihilation (creation) operator b (b^\dagger), corresponding to thermalized quasi-particles, by the Bogoliubov-Valatin transformation, $a_k = c_k b_k + s_{-k}^* b_{-k}^\dagger$; $a_k^\dagger = c_k^* b_k^\dagger + s_{-k} b_{-k}$, where $c_k = \cosh(f_k)$, $s_k = \sinh(f_k)$. The argument, $f_{i,j}(x) = \frac{1}{2} \log \left[\frac{K_{i,j}^\mu(x) u_\mu(x)}{K_{i,j}^{*\nu}(x) u_\nu(x)} \right]$, is the *squeezing parameter*. In terms of the above amplitudes, the complete $\phi\phi$ correlation function can be written as

$$C_2(\mathbf{k}_1, \mathbf{k}_2) = 1 + \frac{|G_c(\mathbf{k}_1, \mathbf{k}_2)|^2}{G_c(\mathbf{k}_1, \mathbf{k}_1)G_c(\mathbf{k}_2, \mathbf{k}_2)} + \frac{|G_s(\mathbf{k}_1, \mathbf{k}_2)|^2}{G_c(\mathbf{k}_1, \mathbf{k}_1)G_c(\mathbf{k}_2, \mathbf{k}_2)}, \quad (1)$$

where the first two terms correspond to the identical particle (HBT) correlation, whereas the first and the last terms represent the correlation function between the particle and its antiparticle, i.e., the squeezed part. The in-medium modified mass, m_* , is related to the asymptotic mass, m , by $m_*^2(|\mathbf{k}|) = m^2 - \delta M^2(|\mathbf{k}|)$, here assumed to be a constant mass-shift.

2. Results

The formulation for both bosons and fermions was initially derived for a static, infinite medium [1, 2]. More recently, it was shown [3] in the bosonic case that, for finite-size systems expanding with moderate flow, the squeezed correlations may survive with sizable strength to be observed experimentally. Similar behavior is expected in the fermionic case. In that analysis, a non-relativistic treatment with flow-independent squeezing parameter was adopted for the sake of simplicity, allowing to obtain analytical results. The detailed discussion is in Ref. [3], where the maximum value of $C_s(\mathbf{k}, -\mathbf{k})$, was studied as a function of the modified mass, m_* , considering pairs with exact back-to-back momentum, $\mathbf{k}_1 = -\mathbf{k}_2 = \mathbf{k}$ (in the identical particle case, this procedure would be analogous to study the behavior of the intercept of the HBT correlation function). Although illustrating many points of theoretical interest, this study in terms of the unobserved shifted mass and exactly back-to-back momenta was not helpful for motivating the experimental search of the BBC's. A more realistic analysis would involve combinations of the momenta of the individual particles, $(\mathbf{k}_1, \mathbf{k}_2)$, into the average momentum of the pair, $\mathbf{K} = \frac{1}{2}(\mathbf{k}_1 + \mathbf{k}_2)$. Since the maximum of the BBC effect is reached when $\mathbf{k}_1 = -\mathbf{k}_2 = \mathbf{k}$, this would correspond to investigate the squeezed correlation function, $C_s(\mathbf{k}_1, \mathbf{k}_2) = C_s(\mathbf{K}, \mathbf{q})$, close to $|\mathbf{K}| = 0$.

For a hydrodynamical ensemble, both the chaotic and the squeezed amplitudes, G_c and G_s , respectively, can be written in a special form derived in [5] and developed in [1, 3]. Therefore, within a non-relativistic treatment with flow-independent squeezing parameter, the squeezed amplitude is written as in [3], i.e., $G_s(\mathbf{k}_1, \mathbf{k}_2) = \frac{E_{1,2}}{(2\pi)^{\frac{3}{2}}} c_0 s_0 \left\{ R^3 \exp\left[-\frac{R^2}{2}(\mathbf{k}_1 + \mathbf{k}_2)^2\right] + 2n_0^* R_*^3 \exp\left[-\frac{(\mathbf{k}_1 - \mathbf{k}_2)^2}{8m_* T}\right] \exp\left[-\frac{im\langle u \rangle R(\mathbf{k}_1 + \mathbf{k}_2)^2}{2m_* T_*}\right] \exp\left[-\left(\frac{1}{8m_* T_*} + \frac{R_*^2}{2}\right)(\mathbf{k}_1 + \mathbf{k}_2)^2\right] \right\}$, and the spectrum, as $G_c(\mathbf{k}_i, \mathbf{k}_i) = \frac{E_{i,i}}{(2\pi)^{\frac{3}{2}}} \left\{ |s_0|^2 R^3 + n_0^* R_*^3 (|c_0|^2 + |s_0|^2) \exp\left(-\frac{\mathbf{k}_i^2}{2m_* T_*}\right) \right\}$, where $R_* = R\sqrt{T/T_*}$ and $T_* = T + \frac{m^2 \langle u \rangle^2}{m_*}$ [3, 6]. We adopt here $\hbar = c = 1$.

Inserting these expressions into Eq. (1) and considering the region where the HBT correlation is not relevant, we obtain the results shown in Figure 1. Part (a) shows the squeezed correlation as a function of $2\mathbf{K} = (\mathbf{k}_1 + \mathbf{k}_2)$, for several values of $\mathbf{q} = (\mathbf{k}_1 - \mathbf{k}_2)$. The top plot shows results expected in the case of a instant emission of the $\phi\phi$ correlated pair. If, however, the emission happens in a finite interval, the second term in Eq. (1) is multiplied by a reduction factor, in this case expressed by a Lorentzian ($F(\Delta t) = [1 + (\omega_1 + \omega_2)^2 \Delta t^2]^{-1}$), i.e., the Fourier transform of an exponential emission. The result is shown in the plot in the middle of Figure 1(a). We see that this represents a dramatic reduction in the signal, even though its strength is sizable for being observed experimentally. If the system expands with radial flow ($\langle u \rangle = 0.5$), the result is shown in the plot at the bottom of

Figure 1(a), again considering that the ϕ 's are emitted during a finite period of time, $\Delta t = 2 \text{ fm}/c$. We see that, in the absence of flow, the squeezed correlation signal grows faster for higher values $|\mathbf{q}|$ than the corresponding case in the presence of flow. However, this last one is stronger in all the investigated $|\mathbf{q}|$ region, showing that the presence of radial flow enhances the signal. The sensitivity of the squeezed-pair correlation to the size of the region where the mass-shift occurs is shown in Figure 1(b) for two values of radii, $R = 7 \text{ fm}$ and $R = 3 \text{ fm}$, keeping $|\mathbf{q}_{12}| = 2.0 \text{ GeV}/c$ fixed. The differences are reflected in the inverse width of the curves, plotted as a function of $2|\mathbf{K}|$. In case of no in-medium mass modification, the squeezed correlation functions would be unity for all values of $2|\mathbf{K}|$ in both plots.

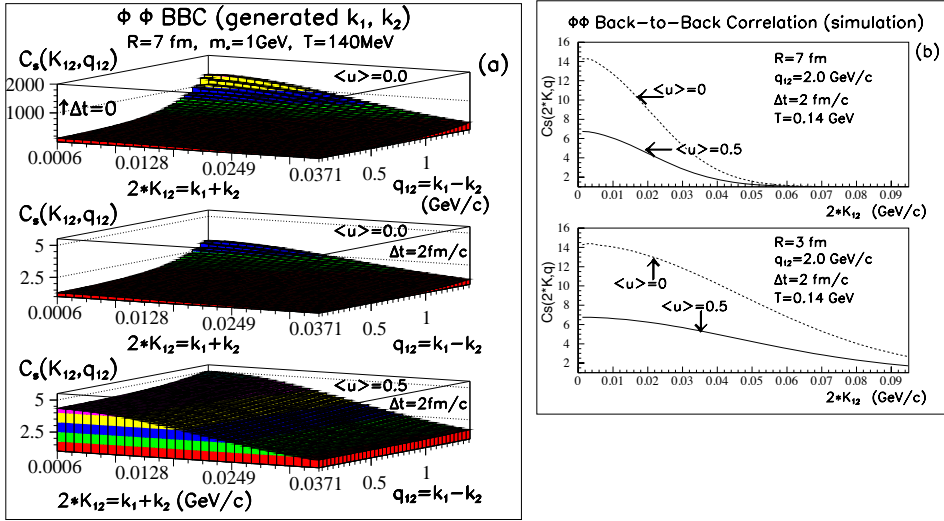


Fig. 1. In part (a), the squeezed-pair correlations are shown, illustrating the effects of flow and finite emission times. Part (b) shows the response of the BBC function to the size of the squeezing region, with $R = 7 \text{ fm}$ (top) and $R = 3 \text{ fm}$ (bottom).

In the case of the squeezed correlations of K^+K^- pairs, we show in Figure 2(a) results for the generated momenta of the pairs within the narrow interval $|\mathbf{K}_{12}| \leq 10 \text{ MeV}/c$, by plotting the squeezed correlation, $C_s(m_*, \mathbf{q}_{12})$ versus m_* and \mathbf{q}_{12} . For the kaons, we can fix the value of the shifted mass to be $m_* \approx 650 \text{ MeV}$, corresponding to one of the maxima in Figure 2(a), and then procedure similarly to what was done in the $\phi\phi$ case. The result is shown in Figure 3 of Ref.[7]. Also in this case the intensity of the squeezed

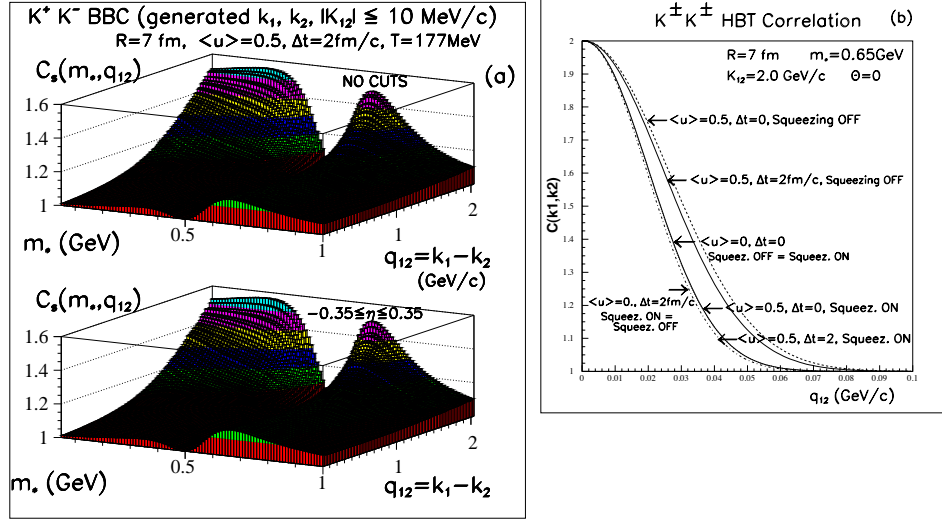


Fig. 2. Part (a) shows the behavior of the correlation function with the in-medium modified mass and the relative momentum of the pair. Part (b) shows the HBT correlation function when squeezing and radial flow are either absent or present.

correlation would be large enough to be searched for experimentally.

Next, we investigate how the behavior of the identical particle correlations could be affected in case of in-medium mass modification, since the femtoscopic correlation function also depends on the squeezing factor, $f_{i,j}(m, m_*)$. The HBT correlation function is obtained by inserting the chaotic amplitude, $G_c(\mathbf{k}_1, \mathbf{k}_2) = \frac{E_{1,2}}{(2\pi)^{\frac{3}{2}}} \left\{ |s_0|^2 R^3 \exp\left[-\frac{R^2}{2}(\mathbf{k}_1 - \mathbf{k}_2)^2\right] + n_0^* R_*^3 (|c_0|^2 + |s_0|^2) \exp\left[-\frac{(\mathbf{k}_1 + \mathbf{k}_2)^2}{8m_* T_*}\right] \exp\left[-\left(\frac{im\langle u \rangle R}{2m_* T_*}\right)(\mathbf{k}_1^2 - \mathbf{k}_2^2)\right] \exp\left[-\left(\frac{1}{8m_* T_*} + \frac{R_*^2}{2}\right)(\mathbf{k}_1 - \mathbf{k}_2)^2\right] \right\}$, together with the expression for the spectrum, into Eq.(1). We use the case of identical $K^\pm K^\pm$ pairs as illustration, as seen in Figure 2(b). The investigation is extended to both the cases of instant emission ($\Delta t = 0$) and finite emission ($\Delta t = 2\text{fm}/c$). In this figure, we can see the well-known result corresponding to the narrowing of the femtoscopic correlation function with increasing emission times, as well as the broadening the curve with flow in the absence of squeezing, as expected. However, if the squeezing originated in the mass-shift is present, its effects tend to oppose to those of flow (for large $|\mathbf{K}|$, it practically cancels the broadening of the correlation function due to flow), another striking indication of mass-modification, even in HBT!

3. Conclusions

In the present work we suggest an effective way to search for the back-to-back squeezed correlations in heavy ion collisions at RHIC, and later at LHC energies, by investigating the squeezed correlation function, $C_s(\mathbf{k}_1, \mathbf{k}_2) = C_s(\mathbf{K}, \mathbf{q})$, in terms of $2\mathbf{K}_{1,2} = (\mathbf{k}_1 + \mathbf{k}_2)$, for different values of $\mathbf{q}_{1,2} = (\mathbf{k}_1 - \mathbf{k}_2)$.

We showed that, in the presence of flow, the signal is stronger over the momentum regions analyzed in the plots, suggesting that flow may help to effectively discover the BBC signal experimentally. Another important point that we find, within this simplified model and in the non-relativistic limit considered here, is that the squeezing would distort significantly the HBT correlation function as well, tending to oppose to the flow effects on those curves, practically neutralizing it for large values of $|\mathbf{K}|$.

The analysis in terms of the variable $2\mathbf{K}$ would not be suited for a genuine relativistic treatment. In this case, however, a momentum variable could be constructed, as $Q_{back} = (\omega_1 - \omega_2, \mathbf{k}_1 + \mathbf{k}_2) = (q^0, 2\mathbf{K})$. In fact, it would be preferable to redefine this variable as $Q_{bbc}^2 = -(Q_{back})^2 = 4(\omega_1\omega_2 - K^\mu K_\mu)$, whose non-relativistic limit is $Q_{bbc}^2 \rightarrow (2\mathbf{K})^2$, as discussed in Ref.[6, 7]. Finally, it is important to emphasize that all the effects and signals discussed here would exist only if the particles analyzed had their masses modified by interactions in the hot and dense medium.

Acknowledgments

SSP is very grateful to the Organizing Committee of the WPCF 2008 for the kind support to attend the workshop. DMD thanks CAPES and FAPESP for the financial support.

REFERENCES

- [1] M. Asakawa M, T. Csörgő and M. Gyulassy *Phys. Rev. Lett.* **83**, 4013 (1999).
- [2] P. K. Panda, T. Csörgő, Y. Hama, G. Krein and Sandra S. Padula, *Phys. Lett B* **512**, 49 (2001).
- [3] Sandra S. Padula, Y. Hama, G. Krein, P. K. Panda and T. Csörgő, *Phys. Rev. C* **73**, 044906 (2006).
- [4] M. Gyulassy, S. K. Kaufmann, and L. W. Wilson, *Phys. Rev. C* **20**, 2267 (1979).
- [5] A. Makhlin and Yu. Sinyukov, *Sov. J. Nucl. Phys.* **46**, 354 (1987); Yu. Sinyukov, *Nucl. Phys. A* **566**, 589c (1994).
- [6] Sandra S. Padula, O. Socolowski Jr., T. Csörgő, M. I. Nagy, Proc. Quark Matter 2008, *J. Phys. G: Nucl. Part. Phys.* **35**, 104141 (2008).
- [7] Sandra S. Padula, O. Socolowski Jr. and Danuce M. Dudek, arXiv:0812.1784v1[nucl-th], to be published in the Proc. of the XXXVIII International Symposium on Multiparticle Dynamics (ISMD 2008).